COMBINED COMPETITIVE (PRELIMINARY) EXAMINATION, 2013

Serial No. $\square$

Time Allowed : Two Hours

## STATISTICS

Code No. 21


Maximum Marks : 300

## INSTRUCTIONS

1. IMMEDIATELY AFTER THE COMMENCEMENT OF THE EXAMINATION, YOU SHOULD CHECK THAT THIS TEST BOOKLET DOES NOT HAVE ANY UNPRINTED OR TORN OR MISSING PAGES OR ITEMS, ETC. IF SO, GET IT REPLACED BY A COMPLETE TEST BOOKLET.
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$\qquad$
4. This Booklet contains 100 items (questions). Each item comprises four responses (answers). You will select one response which you want to mark on the Response Sheet. In case you feel that there is more than one correct response, mark the response which you consider the best. In any case, choose ONLY ONE response for each item.
5. In case you find any discrepancy in this test booklet in any question(s) or the Responses, a written representation explaining the details of such alleged discrepancy, be submitted within three days, indicating the Question No(s) and the Test Booklet Series, in which the discrepancy is alleged. Representation not received within time shall not be entertained at all.
6. You have to mark all your responses ONLY on the separate Response Sheet provided. See directions in the Response Sheet.
7. All items carry equal marks. Attempt ALLitems. Your total marks will depend only on the number of correct responses marked by you in the Response Sheet.
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9. While writing Centre, Subject and Roll No. on the top of the Response Sheet in appropriate boxes use "ONLY BALL POINT PEN".
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## ROUGH WORK

1. Given $P(A)=0.3, P(B)=p$ and $P(A \cup B)=0.58$ then events $A$ and $B$ will be independent if $p$ is :
(A) 0.4
(B) 0.3
(C) 0
(D) none of these
2. A problem in Statistics is given to 3 students whose chances of solving it independently are $\frac{1}{2}, \frac{1}{3}$ and $\frac{1}{4}$ respectively, then the probability that the problem will be solved is :
(A) $\frac{1}{4}$
(B) $\frac{2}{3}$
(C) $\frac{3}{4}$
(D) 1
3. If 3 letters are to be put in 3 addressed envelopes, the probability that none of the letters are in the correct envelope is :
(A) 0
(B) $\frac{1}{6}$
(C) $\frac{1}{3}$
(D) $\frac{1}{2}$
4. If $\mathrm{x}_{i}, i=1,2,3$ are independently distributed as $\operatorname{Uniform} \mathrm{U}(0,1)$, then the probability that exactly 2 of the 3 variables exceed $\frac{1}{3}$ is :
$\mathrm{P}(\mathrm{AB}) \leq \mathrm{P}(\mathrm{A})+\mathrm{P}(\mathrm{B})$
(A) $\frac{1}{3}$
(B) $\frac{2}{3}$
(C) $\frac{2}{9}$
(D) $\frac{4}{9}$
5. For 2 events $A$ and $B$, it is given that :
(i) $P(A B) \geq 1-P(\bar{A})-P(\bar{B})$
(ii) $\mathrm{P}(\mathrm{AB}) \geq \mathrm{P}(\mathrm{A})+\mathrm{P}(\mathrm{B})-1$
(iii)

Out of these :
(A) Only (i) is correct
(B) Only (ii) is correct
(C) Only (iii) is correct
(D) All the three are correct

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6. In a binomial distribution $B(n, p)$

$$
\begin{aligned}
& \text { mean }- \text { variance }=1 \\
& (\text { mean })^{2}-(\text { variance })^{2}=11
\end{aligned}
$$

then $p$ is :
(A)
(B) $\frac{5}{6}$
(C) $\frac{1}{3}$
(D) $\frac{2}{3}$
7. Let X has continuous distribution with cumulative distribution function (cdf) $\mathrm{F}(\mathrm{x})$, then the distribution of $Y=F(X)$ is :
(A) Exponential
(B) Uniform
(C) Normal
(D) None of these
8. The mean and variance of a random variable X are same then the distribution of X is :
(A) Binomial
(B) Poisson
(C) Geometric
(D) Normal
9. Let X has Poisson $\mathrm{P}(\lambda)$ distribution, with

$$
P(x=1)=P(x=2)
$$

then the variance of $x$ is :
(A) 1
(B) 2
(C) 3
(D) None of these
10. Let $\mathrm{E}(\mathrm{x})=3$ and $\mathrm{E}\left(\mathrm{x}^{2}\right)=13$, then the Chebyshev's lower bound for $\mathrm{P}[-2<\mathrm{x}<8]$ is :
(A) 1
(B) $\frac{4}{25}$
(C) $\frac{21}{25}$
(D) None of these
11. The probability that a non-leap year will have 53 Sundays is :
(A) $\frac{1}{7}$
(B) $\frac{2}{7}$
(C) $\frac{5}{7}$
(D) $\frac{6}{7}$
12. If $X$ and $Y$ have the joint probability mass function :

$$
f(x, y)=c\left(\frac{1}{2}\right)^{x}\left(\frac{1}{3}\right)^{y}, x, y=0,1,2 \ldots
$$

then the value of $c$ is :
(A) $\frac{1}{2}$
(B) $\frac{1}{3}$
(C) 2
(D) 3
13. Let X has normal $\mathrm{N}\left(\mu, \sigma^{2}\right)$ distribution. If $\mathrm{P}[\mathrm{x} \leq 15]=\frac{1}{2}$, then $\mu$ is :
(A) 10
(B) 15
(C) 20
(D) None of these
14. Let the probability mass function of X be :

$$
\mathrm{P}(\mathrm{X}=\mathrm{x})=\binom{3}{\mathrm{x}}\left(\frac{1}{8}\right), \mathrm{x}=0,1,2,3
$$

with (i) moment generating function $(\mathrm{mgf})=\frac{1}{8}\left(1+\mathrm{e}^{\mathrm{t}}\right)^{3}$
(ii) mean $=3 / 2$

Out of these:
(A) Only (i) is correct
(B) Only (ii) is correct
(C) Both (i) and (ii) are correct
(D) None is correct
15. If the moment generating function (mgf) of $X$ be $M(t)=\frac{\left[e^{t}-1\right]}{t}$ then the variance of $X$ is :
(A) $\frac{1}{2}$
(B) $\frac{1}{3}$
(C) $\frac{1}{12}$
(D) None of these
16. If the joint pdf of $(X, Y)$ be
$\mathrm{f}(\mathrm{x}, \mathrm{y})=2,0<\mathrm{y}<\mathrm{x}<1$ then the conditional expectation $\mathrm{E}[\mathrm{Y} \mid \mathrm{X}=\mathrm{x}]$ is :
(A) $\frac{x}{2}$
(B) $\frac{\mathrm{x}^{2}}{2}$
(C) $\frac{1}{\mathrm{x}}$
(D) None of these
17. Which one of the following distributions has memory less property?
(A) Normal
(B) Binomial
(C) Exponential
(D) Uniform
18. A box contains 'a' white and 'b' black balls. 'c' balls are drawn without replacement. Then the expected number of white balls drawn is :
(A) $\frac{a c}{a+b}$
(B) $\frac{b c}{a+b}$
(C) $\frac{a}{a+b}$
(D) None of these
19. For a negative binomial $\mathrm{NB}(\mathrm{r}, \mathrm{p})$ distribution :
(A) mean $>$ variance
(B) mean < variance
(C) mean = variance
(D) not definite
20. Let $X$ and $Y$ are independent Poisson variates then the conditional distribution of $X$ given $(\mathrm{X}+\mathrm{Y})$ is :
(A) Poisson
(B) Binomial
(C) Geometric
(D) None of these
21. Let $\mathrm{x}_{1}$ and $\mathrm{x}_{2}$ be independently binomially distributed as $\mathrm{B}\left(\mathrm{n}_{1}, \mathrm{p}\right)$ and $\mathrm{B}\left(\mathrm{n}_{2}, 1-\mathrm{p}\right)$ respectively then $B\left(n_{1}+n_{2}, p\right)$ will be distribution of :
(A) $\mathrm{x}_{1}+\mathrm{x}_{2}$
(B) $\mathrm{x}_{1}+\mathrm{n}_{2}-\mathrm{x}_{2}$
(C) $x_{2}+n_{1}-x_{1}$
(D) None of these
22. Let $(\mathrm{X}, \mathrm{Y})$ has bivariate normal $\mathrm{BN}(4,2,16,25,3 / 5)$ then the conditional mean of Y given $\mathrm{X}=8$ is :
(A) 5
(B) 4
(C) 2
(D) $\frac{98}{25}$
23. If x has exponential distribution with mean 2 , then $\mathrm{P}[\mathrm{x}<2]$ is :
(A) $\mathrm{e}^{-1}$
(B) $1-\mathrm{e}^{-1}$
(C) $\mathrm{e}^{-2}$
(D) None of these
24. Let $\left\{X_{K}\right\}$ be a sequence of independent random variables with

$$
\mathrm{P}\left(\mathrm{X}_{\mathrm{K}}= \pm \mathrm{K}^{\alpha}\right)=\frac{1}{2}
$$

then Weak Law of Large Numbers (WLLN) holds if :
(A) $\alpha<\frac{1}{2}$
(B) $\frac{1}{2}<\alpha<1$
(C) $\alpha>1$
(D) None of these

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25. If the pdf of normal $N\left(\mu, \sigma^{2}\right)$ distribution be

$$
f(x)=e^{\frac{-x^{2}}{4}+\frac{3}{2} x}
$$

then $\left(\mu, \sigma^{2}\right)$ are :
(A) $(2,3)$
(B) $(3,2)$
(C) $(3,1)$
(D) None of these
26. The mean of first n natural numbers is :
(A) $\frac{\mathrm{n}(\mathrm{n}+1)}{2}$
(B)
(C)
(D) None of these
27. The mean weight of boys in a class is 60 kg and that of girls is 40 kg . If the average weight of the class be 46 kg , then the percentage of boys and girls in the class is :
(A) $(60,40)$
(B) $(40,60)$
(C) $(30,70)$
(D) $(70,30)$
28. The sum of absolute deviations is least when measured from :
(A) mean
(B) median
(C) mode
(D) geometric mean
29. A student pedals from his home to the college at the speed of $10 \mathrm{~km} / \mathrm{hour}$ and back at the speed of $15 \mathrm{~km} /$ hour. Then his average speed in $\mathrm{km} /$ hour is :
(A) 12
(B) 12.2
(C) 12.5
(D) None of these
30. The harmonic mean $(\mathrm{H})$ of two numbers is 4 and their arithmetic mean $(\mathrm{A})$ and geometric mean (G) satisfy $2 \mathrm{~A}+\mathrm{G}^{2}=27$, then the numbers are :
(A) $(1,3)$
(B) $(6,3)$
(C) $(9,5)$
(D) $(12,7)$
31. In a moderately asymmetric distribution the median and mean are respectively 42 and 40 , then the mode is :
(A) 40
(B) 42
(C) 44
(D) 46
32. The relation between arithmetic mean (A), geometric mean $(\mathrm{G})$ and harmonic mean $(\mathrm{H})$ is :
(A) $\mathrm{A}>\mathrm{H}>\mathrm{G}$
(B) A $>$ G $>\mathrm{H}$
(C) G $>$ A $>\mathrm{H}$
(D) $\mathrm{H}>$ G $>\mathrm{A}$

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33. Let X be a random variable with mean $\mu$ and median m then $\mathrm{E}(\mathrm{x}-\mathrm{b})^{2}$ is least if :
(A) $\mathrm{b}=0$
(B) $\mathrm{b}=\mathrm{m}$
(C) $\mathrm{b}=\mu$
(D) None of these
34. A discrete random variable takes values -1 and 1 with respective probability $p$ and $q$. If $\mathrm{E}(\mathrm{x})=\frac{3}{5}$, then the standard deviation of X is :
(A) $\frac{4}{5}$
(B) $\frac{16}{25}$
(C) $-\frac{4}{5}$
(D) None of these
35. The first 4 moments about a number ' 4 ' are $1,4,10,45$, then the mean and variance are :
(A) $(1,4)$
(B) $(5,3)$
(C) $(5,4)$
(D) None of these
36. If the possible values of X are $1,2,3 \ldots$ then $\mathrm{E}(\mathrm{X})$ is :
(A) $\mathrm{P}(\mathrm{X} \geq \mathrm{n})$
(B) $\mathrm{P}(\mathrm{X}<\mathrm{n})$
(C) $\sum_{n=1}^{\infty} P(X \geq n)$
(D) $\sum_{\mathrm{n}=1}^{\infty} \mathrm{P}(\mathrm{X}<\mathrm{n})$
37. If two regression lines be :

$$
\begin{aligned}
& 3 x+5 y=8 \\
& 2 x+5 y=7
\end{aligned}
$$

then the correlation coefficient between $(\mathrm{X}, \mathrm{Y})$ is :
(A) $2 / 3$
(B) $\sqrt{2 / 3}$
(C) $-\sqrt{2 / 3}$
(D) 0
38. The means and variances of two independent random variables $X$ and $Y$ are same, then the correlation between $(\mathrm{X}, \mathrm{X}-\mathrm{Y})$ is :
(A) 0
(B) $\frac{1}{\sqrt{2}}$
(C) $-\frac{1}{\sqrt{2}}$
(D) 1
39. If $b_{x y}$ and $b_{y x}$ be two regression coefficients and if $b_{x y}>1$, then:
(A) $b_{y x}>1$
(B) $0<b_{y x}<1$
(C) $\mathrm{b}_{\mathrm{yx}}<0$
(D) not definite

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40. If correlation between $(\mathrm{X}, \mathrm{Y})$ be 0.4 , then correlation between $(-2 \mathrm{X}+1,3 \mathrm{Y}+2)$ will be :
(A) 0.4
(B) -0.4
(C) 0.0
(D) 1.0
41. For a $\chi^{2}$-distribution:
(A) mean = variance
(B) 2 mean = variance
(C) mean = 2 variance
(D) none of these
42. If X has uniform $\mathrm{U}(0,1)$ distribution, then the pdf of the $\mathrm{r}^{\text {th }}$ order statistic is :
(A) Exponential
(B) Beta
(C) Uniform
(D) None of these
43. In a frequency distribution, the fourth central moment is double of the [variance] $]^{2}$ then the distribution is:
(A) Leptokurtic
(B) Platykurtic
(C) Mesokurtic
(D) All of these
44. Let x has $\mathrm{F}(\mathrm{m}, \mathrm{n})$ distribution, then the distribution of $\frac{1}{\mathrm{x}}$ will be :
(A) $\mathrm{F}(\mathrm{m}, \mathrm{n})$
(B) $\mathrm{F}(\mathrm{n}, \mathrm{m})$
(C) $\chi^{2}$
(D) t
45. Let x has t -distribution with n degrees of freedom. If $\mathrm{n}=1$, then the distribution of t reduces to :
(A) Normal
(B) Cauchy
(C) F
(D) None of these
46. The pdf of the first order statistic in $f(x, \theta)=\frac{1}{\theta} e^{-\frac{x}{\theta}}, x>0$ is :
(A) Exponential
(B) Uniform
(C) Beta
(D) None of these
47. The mean of first order statistic in Uniform $\mathrm{U}(0,1)$

$$
f(x)=1 \quad 0<x<1
$$

is:
(A) $\frac{1}{n}$
(B) $\frac{1}{\mathrm{n}+1}$
(C) $\frac{1}{\mathrm{n}-1}$
(D) $\frac{\mathrm{n}}{\mathrm{n}^{2}-1}$

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48. If for two attributes $A$ and $B \frac{(A B)}{(B)}=\frac{(A \beta)}{\beta}$, then $A$ and $B$ are :
(A) independent
(B) positively associated
(C) negatively associated
(D) no conclusion
49. If the regression line of $Y$ on $X$ be

$$
y=a x+b
$$

then a is:
(A) $\rho \frac{\sigma_{y}}{\sigma_{x}}$
(B) $\rho \frac{\sigma_{x}}{\sigma_{y}}$
(C) $\rho$
(D) None of these
where
50. If range of correlation coefficient be $(0,1)$ then the correlation is :
(A) Partial
(B) Multiple
(C) Rank
(D) Simple
51. An unbiased estimator of $\theta$ in $f(x, \theta)=\frac{1}{\theta}, 0<x<\theta$ is :
(A) Sample mean
(B) Sample median
(C) Largestobservation
(D) Double of the sample mean
52. Sufficient statistic of $\theta$ in $f(x, \theta)=e^{-(x-\theta)}, \quad x \geq \theta$ is :
(A) $\min \left(\mathrm{x}_{1}, \ldots ., \mathrm{x}_{\mathrm{n}}\right)$
(B) $\max \left(\mathrm{x}_{1}, \ldots, \mathrm{x}_{\mathrm{n}}\right)$
(C) sample mean
(D) sample median
53. The minimum variance unbiased estimator (mvue) of $\theta^{2}$ in normal $\mathrm{N}(\theta, 1)$ distribution is :
(A) $\overline{\mathrm{x}}^{2}-\frac{1}{\mathrm{n}}$
(B) $\overline{\mathrm{x}}^{2}+\frac{1}{\mathrm{n}}$
(C) $\bar{x}^{2}$
(D) None of these
54. Maximum likelihood estimator (mle) of $\sigma^{2}$ in normal $N\left(\mu, \sigma^{2}\right)$ distribution when $\mu$ is unknown is :
(A)
(B) $\frac{1}{\mathrm{n}-1} \sum_{1}^{\mathrm{n}}\left(\mathrm{x}_{\mathrm{i}}-\overline{\mathrm{x}}\right)^{2}$
(C) $\frac{1}{\mathrm{n}} \sum_{1}^{\mathrm{n}} \mathrm{x}_{\mathrm{i}}^{2}$
(D) $\frac{1}{\mathrm{n}} \sum_{1}^{\mathrm{n}}\left(\mathrm{x}_{\mathrm{i}}-\mu\right)^{2}$

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55. If $x_{1}, x_{2}$ and $x_{3}$ are independently distributed with mean $\theta$, then

$$
\mathrm{T}=\mathrm{x}_{1}+2 \mathrm{x}_{2}+\lambda \mathrm{x}_{3}
$$

is unbiased estimator of $\theta$ if $\lambda$ is :
(A) 1
(B) -1
(C) 0
(D) -2
56. Cramer-Rao Lower Bound (CRLB) for the variance of an unbiased estimator $\theta$ from Poisson $P(\theta)$ is :
(A) $\frac{\theta}{n}$
(B) $\frac{\theta^{2}}{\mathrm{n}}$
(C) $\theta$
(D) $\theta^{2}$
57. Maximum likelihood estimator (mle) of $\theta$ in

$$
\mathrm{f}(\mathrm{x}, \theta)=\frac{1}{2} \mathrm{e}^{-|x-\theta|}, \quad-\infty<\mathrm{x}<\infty
$$

is:
(A) Sample mean
(B) $\operatorname{Max}\left(\mathrm{x}_{1}, \ldots, \mathrm{x}_{\mathrm{n}}\right)$
(C) $\operatorname{Min}\left(\left(\mathrm{x}_{1}, \ldots, \mathrm{x}_{\mathrm{n}}\right)\right.$
(D) Sample median
58. Confidence interval for $\sigma^{2}$ in normal $\mathrm{N}\left(\mu, \sigma^{2}\right)$ distribution is based on the distribution :
(A) t
(B) normal
(C) $\chi^{2}$
(D) F
59. Let X has Poisson $\mathrm{P}(\theta)$ distribution, then mle of $\mathrm{e}^{\theta}$ is :
(A) $\mathrm{e}^{\overline{\mathrm{x}}}$
(B) $\overline{\mathrm{x}}$
(C)
(D) None of these
60. The mvue of $\theta$ in

$$
\mathrm{f}(\mathrm{x}, \theta)=\frac{1}{\theta}, \quad 0<\mathrm{x}<\theta
$$

is:
(A) $2 \overline{\mathrm{X}}$
(B)
(C) $\frac{\mathrm{n}+1}{\mathrm{n}} \mathrm{X}_{(\mathrm{n})}$
(D) $\frac{\mathrm{n}}{\mathrm{n}+1} \mathrm{X}_{(\mathrm{n})}$
where $\mathrm{X}_{(\mathrm{n})}=\max \left(\mathrm{X}_{1}, \ldots, \mathrm{X}_{\mathrm{n}}\right)$
61. Which of the following statements is not true ?
(A) consistency does not imply unbiasedness
(B) unbiasedness does not imply consistency
(C) mle is function of sufficient statistic
(D) mle is unbiased
62. The moment estimator of $\sigma^{2}$ in normal $\mathrm{N}\left(\mu, \sigma^{2}\right)$ distribution, when $\mu$ is unknown is :
(A) $\frac{1}{\mathrm{n}} \sum_{1}^{\mathrm{n}}\left(\mathrm{x}_{\mathrm{i}}-\overline{\mathrm{x}}\right)^{2}$
(B) $\frac{1}{\mathrm{n}-1} \sum_{1}^{\mathrm{n}}\left(\mathrm{x}_{\mathrm{i}}-\overline{\mathrm{x}}\right)^{2}$
(C) $\frac{1}{\mathrm{n}} \sum_{1}^{\mathrm{n}} \mathrm{x}_{\mathrm{i}}{ }^{2}$
(D) none of these
63. For the pdf

$$
\mathrm{f}(\mathrm{x}, \theta)=\frac{1}{\theta}, \quad 0<\mathrm{x}<\theta
$$

the moment estimator of $\theta$ is :
(A) $\bar{x}$
(B)
(C)
(D) none of these
64. Let $\mathrm{x}_{1}, \mathrm{x}_{2}$ be a random sample of size 2 from the distribution

$$
\mathrm{f}(\mathrm{x}, \theta)=\theta \mathrm{x}^{\theta-1}, 0<\mathrm{x}<1
$$

then sufficient statistic for $\theta$ is :
(A) $\mathrm{x}_{1} \mathrm{x}_{2}$
(B) $\mathrm{x}_{1}+\mathrm{x}_{2}$
(C) $x_{1}-x_{2}$
(D) $\frac{\mathrm{x}_{1}}{\mathrm{x}_{2}}$
65. MLE are always:
(A) unbiased
(B) unique
(C) consistent
(D) none of these
66. Neyman-Pearson lemma is used for finding Most Powerful (MP) test for :
(A) Simple Vs simple hypotheses
(B) Simple Vs composite hypotheses
(C) Composite Vs simple hypotheses
(D) Composite Vs composite hypotheses
67. For an exponential distribution

$$
f(x, \theta)=\frac{1}{\theta} \mathrm{e}^{-x / 6}, x>0, \theta>0
$$

the hypothesis to be tested is

$$
\mathrm{H}_{0}: \theta=1 \quad \mathrm{H}_{1}: \theta=2
$$

If on the basis of a single observation critical region be $x \geq 4$ then the size of the test is :
(A) $1-\overline{\mathrm{e}}^{2}$
(B) $1-\overline{\mathrm{e}}^{4}$
(C) $\overline{\mathrm{e}}^{2}$
(D) $\overline{\mathrm{e}}^{4}$

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68. If $n$ is the sample size, $\mu$ is the population mean and $\sigma^{2}$ is the population variance, then the standard error of sample mean is :
(A) $\sigma$
(B) $\sigma / n$
(C) $\sigma / \sqrt{\mathrm{n}}$
(D) $\sigma / 2 n$
69. Let $X$ has normal $N\left(\mu, \sigma^{2}\right)$ distribution where both $\mu$ and $\sigma^{2}$ are unknown. Then the simple hypothesis is:
(A) $\mathrm{H}_{0}: \sigma=5$
(B) $\mathrm{H}_{0}: \mu=10$
(C) $\mathrm{H}_{0}: \mu=5, \sigma=1$
(D) $\mathrm{H}_{0}: \mu \neq 5, \sigma=1$
70. Which of the following is not related to probability of Type I error ?
(A) $\alpha$
(B) $\beta$
(C) level of significance
(D) size of the test
71. The number of runs in XYY XYXX is:
(A) 2
(B) 3
(C) 4
(D) 5
72. The expected value of the runs in Question 71 is :
(A) 3.1
(B) 4
(C) 4.4
(D) 5.2
73. Let

$$
\mathrm{X}: 10,12,7
$$

$\mathrm{Y}: 5,13,9,15$
then the value of Wilcoxon-Mann-Whitney (WMW) statistic is :
(A) 1
(B) 2
(C) 3
(D) 5
74. The distribution of statistic used in sign test is :
(A) Binomial
(B) Poisson
(C) $\chi^{2}$
(D) t
75. The distribution of the statistic used in median test is :
(A) $\chi^{2}$
(B) t
(C) F
(D) Binomial
76. In a simple random sampling without replacement (SRSWOR), the probability of a sample of size $n$ drawn from Nunits is :
(A) $\frac{1}{\mathrm{~N}}$
(B) $\frac{\mathrm{n}}{\mathrm{N}}$
(C) $\frac{1}{\mathrm{n}}$
(D) $\binom{\frac{1}{N}}{\mathrm{n}}$

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77. In SRSWOR, the variance of the sampling mean $\bar{y}, \operatorname{Var}(\bar{y})$, in usual notation is :
(A) $\left(\frac{1-f}{\mathrm{~N}}\right) \mathrm{S}^{2}$
(B) $\left(\frac{1}{\mathrm{n}}+\frac{1}{\mathrm{~N}}\right) \mathrm{S}^{2}$
(C) $\left(\frac{N-n}{N}\right) S^{2}$
(D) $\left(\frac{1-f}{n}\right) S^{2}$
78. The relation between variances ( V ) in usual notation is :
(A) $V_{\text {opt }} \geq V_{\text {prop }} \geq V_{\text {SRS }}$
(B) $\mathrm{V}_{\text {opt }} \geq \mathrm{V}_{\text {SRS }} \geq \mathrm{V}_{\text {prop }}$
(C) $\mathrm{V}_{\text {prop }} \geq \mathrm{V}_{\text {opt }} \geq \mathrm{V}_{\text {SRS }}$
(D) $\mathrm{V}_{\text {SRS }} \geq \mathrm{V}_{\text {prop }} \geq \mathrm{V}_{\text {opt }}$
79. A population consisting of 100 units is divided into two strata, such that $N_{1}=60, N_{2}=40$, $S_{1}=2$ and $S_{2}=3$. If by Neyman allocation $n_{1}=12$, then the sample size n will be :
(A) 24
(B) 12
(C) 6
(D) none of these
80. The coefficient of variation (CV) in a large population is $10 \%$. In order that the CV of the sample mean be $2 \%$ the size of the simple random sample be :
(A) 5
(B) 10
(C) 25
(D) 250
81. In a SRSWOR, if $\bar{y}=50, n=100, N=500$ then the estimated population total is :
(A) 250
(B) 500
(C) 2500
(D) 25000
82. In simple random sampling (SRS), the relation between sampling fraction (f) and finite population correction (fpc) is :
(A) $\mathrm{fpc}=\mathrm{f}$
(B) $\mathrm{fpc}=1-\mathrm{f}$
(C) $\mathrm{fpc}=$
(D) None of these
83. If the variance of sample mean in SRS with and without replacement be $\mathrm{V}_{\mathrm{WR}}$ and $\mathrm{V}_{\mathrm{WOR}}$ respectively and e is
$e=\frac{V_{\text {Wor }}}{V_{\text {WR }}}$ then the value of $e$ is :
(A) $\frac{\mathrm{N}-\mathrm{n}}{\mathrm{N}-1}$
(B)
(C)
(D) $\frac{\mathrm{N}}{\mathrm{N}-\mathrm{n}}$

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84. In a SRSWR from a population of 400 units, the finite population correction ( fpc ) is 0.75 , then the sample size is :
(A) 100
(B) 75
(C) 60
(D) 50
85. If a population consists of a linear trend, then which of the following is correct?
(A) $\operatorname{Var}\left(\overline{\mathrm{y}}_{\mathrm{st}}\right) \leq \operatorname{Var}\left(\overline{\mathrm{y}}_{\text {sys }}\right) \leq \operatorname{Var}\left(\overline{\mathrm{y}}_{\mathrm{R}}\right)$
(B)
(C)
(D)
where $s t=$ Stratified, sys $=$ Systematic and $\mathrm{R}=$ simple random sampling.
86. Under SRSWOR, $n$ units are drawn from N units. If the ratio estimator of the population mean Y be then is :
(A) $\overline{\mathrm{Y}}-\operatorname{cov}\left(\frac{\overline{\mathrm{y}}}{\overline{\mathrm{x}}}, \overline{\mathrm{x}}\right)$
(B) $\overline{\mathrm{Y}}-\operatorname{cov}(\overline{\mathrm{y}}, \overline{\mathrm{x}})$
(C) $\operatorname{cov}\left(\frac{\bar{y}}{\bar{x}}, \bar{x}\right)$
(D) $\operatorname{cov}\left(\frac{\bar{y}}{\bar{x}}, \bar{y}\right)$

Varchyen
(A) $\sum_{\mathrm{h}=1}^{\mathrm{L}}\left(\frac{1}{\mathrm{~N}_{\mathrm{h}}}-\frac{1}{\mathrm{n}_{\mathrm{h}}}\right) \mathrm{W}_{\mathrm{h}}^{2} \mathrm{~S}_{\mathrm{n}}^{2}$
(B) $\sum_{\mathrm{h}=1}^{\mathrm{L}}\left(\frac{1}{\mathrm{n}_{\mathrm{h}}}-\frac{1}{\mathrm{~N}_{\mathrm{h}}}\right) \mathrm{W}_{\mathrm{h}}^{2} \mathrm{~S}_{\mathrm{n}}^{2}$
(C) $\sum_{\mathrm{h}=1}^{\mathrm{L}}\left(\frac{1}{\mathrm{n}_{\mathrm{h}}}-\frac{1}{\mathrm{~N}_{\mathrm{h}}}\right) \mathrm{W}_{\mathrm{h}} \mathrm{S}_{\mathrm{n}}^{2}$
(D) None of these
where $\mathrm{N}=\sum_{1}^{\mathrm{L}} \mathrm{n}_{\mathrm{h}}, \mathrm{n}=\sum_{1}^{\mathrm{L}} \mathrm{n}_{\mathrm{i}}, \mathrm{W}_{\mathrm{h}}=\frac{\mathrm{N}_{\mathrm{h}}}{\mathrm{N}}$.
88. Basic principle of an experimental design is :
(i) Replication
(ii) Randomization
(iii) Local control

Out of these
(A) Only (i) is true
(B) Only (i) and (ii) are true
(C) Only (ii) and (iii) are true
(D) All (i), (ii) and (iii) are true
89. In a $\mathrm{m}^{2}-\mathrm{LSD}$, the degree of freedom of error is :
(A) $\mathrm{m}^{2}-1$
(B) $(\mathrm{m}-1)^{2}$
(C) $(m-1)(m-2)$
(D) None of these
90. In a RBD with 5 treatments and 4 blocks, one observation is missing, therefore in ANOVA table, degree of freedom for error will be :
(A) 12
(B) 11
(C) 10
(D) None of these
91. In a $\mathrm{m}^{2}-\mathrm{LSD}$, if the degree of freedom of treatment and error are same, then the value of m is :
(A) 7
(B) 5
(C) 4
(D) 3
92. The estimate of the missing value $(\mathrm{X})$ in the following RBD :

| Treat. | Block |  |  |  | Total |
| ---: | ---: | ---: | ---: | ---: | :--- |
|  | 1 | 2 | 3 | 4 |  |
| 1 | 6 | 5 | 7 | 8 | 26 |
| 2 | 7 | X | 4 | 5 | $16+\mathrm{X}$ |
| 3 | 8 | 6 | 5 | 9 | 28 |
| Total | 21 | $11+\mathrm{X}$ | 16 | 22 | $70+\mathrm{X}$ |

(A) 3.6
(B) 4.1
(C) 5.5
(D) 7.8
93. In a LSD, relation between no. of replicates $(r)$ and no. of treatments $(t)$ is :
(A) $\mathrm{r}=\mathrm{t}$
(B) $\mathrm{r}>\mathrm{t}$
(C) $\mathrm{r}<\mathrm{t}$
(D) all of these
94. In a RBD, local control is used in $K$ directions, where $K$ is :
(A) 0
(B) 1
(C) 2
(D) 3
95. The interaction effect in a 2-way design can not be studied if the number of observations per cell is:
(A) 1
(B) 2
(C) 3
(D) 4
96. A $2^{3}$-experimental design is arranged in 2 blocks. If the principal block contains treatment combinations
(1), c, ab, abc
then the confounded interaction is :
(A) AB
(B) AC
(C) BC
(D) ABC
97. The number of confounded interactions in a $2^{\mathrm{n}}$-experimental design arranged in $2^{\mathrm{k}}$ blocks is :
(A) $2^{\mathrm{n}-\mathrm{k}}$
(B) $2^{\mathrm{n}-\mathrm{k}}-3$
(C) $2^{\mathrm{k}}-1$
(D) none of these
98. A two-way classification with $m$ observations per cell has $r$ rows and $c$ columns. The degree of freedom for interaction in ANOVA table is :
(A) $\mathrm{m}-1$
(B) $(\mathrm{m}-1)(\mathrm{r}-1)$
(C) $(\mathrm{m}-1)(\mathrm{c}-1)$
(D) $(\mathrm{r}-1)(\mathrm{c}-1)$
99. Local control is completely absent in :
(A) CRD
(B) RBD
(C) LSD
(D) none of these
100. $\mathrm{Am}^{2}-$ LSD is based on incomplete 3-way experimental design because the no. of experimental units are:
(A) m
(B) $\mathrm{m}^{2}$
(C) $\mathrm{m}^{3}$
(D) $\mathrm{m}^{4}$

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## ROUGH WORK

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